

SCHEME OF EVALUATION (Scoring Indicators)

Revision: 2010

Course Code: 1002

Course Title: TECHNICAL MATHEMATICS-I

Qst No.	Scoring Indicator	Split up Score	Sub Total	Total
<u>PART-A</u>				
I	1. $\sin \theta \cdot \sin \theta - \cos \theta \cdot \cos \theta$ $\sin^2 \theta + \cos^2 \theta = 1$	1	2	2
	2. $11 + 7$ $= 18$	1	2	2
	3. $\frac{\sin A}{\cos A} \cdot \frac{\cos A}{\sin A}$ $= 1$	1	2	2
4	$m = \frac{y_2 - y_1}{x_2 - x_1}$ $= \frac{9 - 5}{6 - 4} = \frac{4}{2} = 2$	1	2	2
5.	$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} = 2R$	2	2	2
				10
<u>PART-B</u>				
II	1. $\Delta = 16 \quad \Delta_1 = 32 \quad \Delta_2 = 16 \quad \Delta_3 = -16$ $x = \frac{\Delta_1}{\Delta} = 2 \quad y = \frac{\Delta_2}{\Delta} = 1 \quad z = \frac{\Delta_3}{\Delta} = -1$		6	6
2.	$(A + A^T)^T = A^T + (A^T)^T = A^T + A$ Symmetric $(A - A^T)^T = A^T - (A^T)^T = A^T - A$ skew-symmetric $\frac{A + A^T}{2} + \frac{A - A^T}{2} = \frac{2A}{2} = A$	2	2	6
3	$t_{r+1} = {}^{12}C_r (x^2)^{12-r} \cdot \left(\frac{1}{x}\right)^r$ $= {}^{12}C_r x^{24-3r}$ $24 - 3r = 0 \quad r = 8, \quad t_9 = {}^{12}C_8$	1	2	6
				24

4

$$\begin{aligned}\tan 75 &= \tan (45+30) \\ &= \frac{\tan 45 + \tan 30}{1 - \tan 45 \cdot \tan 30} = \frac{1 + \sqrt{3}}{1 - \sqrt{3}}\end{aligned}$$

$$\cot 75 = \frac{1 - \sqrt{3}}{1 + \sqrt{3}}$$

$$\tan 75 + \cot 75 = \frac{1 + \sqrt{3}}{1 - \sqrt{3}} + \frac{1 - \sqrt{3}}{1 + \sqrt{3}}$$

$$= 4$$

1

2

6

6

1

2

5.

$$\Delta.H.S = 2 \left(bc \cdot \frac{b^2+c^2-a^2}{2bc} + ca \cdot \frac{c^2+a^2-b^2}{2ca} + ab \cdot \frac{a^2+b^2-c^2}{2ab} \right)$$

$$= b^2+c^2-a^2 + c^2+a^2-b^2 + a^2+b^2-c^2$$

$$= \underline{\underline{a^2+b^2+c^2}}$$

2

6

6

1

6

$$a = 3b$$

$$\text{Equation is } \frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{3b} + \frac{y}{b} = 1$$

$$x + 3y = 3b$$

This line passes through $(-6, 3)$

$$-6 + 3 \cdot 3 = 3b$$

$$b = 1$$

$$a = 3$$

$$\therefore \frac{x}{3} + \frac{y}{1} = 1$$

$$\underline{\underline{x + 3y - 3 = 0}}$$

1

1

1

1

1

1

6

6

7

$$\Delta = \begin{vmatrix} 3 & 1 \\ 2 & -1 \end{vmatrix} = -5$$

$$\Delta_1 = \begin{vmatrix} 2 & 1 \\ 3 & -1 \end{vmatrix} = -5$$

$$\Delta_2 = \begin{vmatrix} 3 & 2 \\ 2 & 3 \end{vmatrix} = 5$$

$$x = 1 \quad y = -1$$

Third line is $kx + 2y - 3 = 0$

$$k = 5$$

1

1

1

1

1

6

6

PART-C

(ii)

1.

$\Delta = 4$

Cofactor matrix = $\begin{bmatrix} 0 & 2 & -2 \\ -2 & 4 & -2 \\ 2 & -2 & 4 \end{bmatrix}$

Adjoint matrix

$\begin{bmatrix} 0 & -2 & 2 \\ 2 & 4 & -2 \\ -2 & -2 & 4 \end{bmatrix}$

$A^{-1} = \frac{Adj A}{|A|}$

$= \frac{\begin{bmatrix} 0 & -2 & 2 \\ 2 & 4 & -2 \\ -2 & -2 & 4 \end{bmatrix}}{4}$

1
1
1
1
5
5

2.

$BC = \begin{bmatrix} 1+6 & 2+0 & 3-6 & -4-3 \\ 0+4 & 0+0 & 0-4 & 0-2 \\ -1+8 & -2+0 & -3-8 & 4-4 \end{bmatrix}$

$= \begin{bmatrix} 7 & 2 & -3 & -7 \\ 4 & 0 & -4 & -2 \\ 7 & -2 & -11 & 0 \end{bmatrix}$

3
5
5
2

3.

$3(6-18) - 1(6x-6x^2) + 9(6x-2x^2) = 0$

$-12x^2 + 48x - 36 = 0$

$x^2 - 4x + 3 = 0$

$(x-1)(x-3) = 0$

$x=1$ or $x=3$

1
1
5
5
1

(iii)

1.

$\begin{vmatrix} k & 3 & -5 \\ 5 & -1 & 3 \\ 7 & k & -2 \end{vmatrix} = 0$

$3k^2 + 23k - 58 = 0$

$k=2$

1
5
5
2
2

2.

$A^{-1} = \begin{bmatrix} 3 & 0 \\ 1 & 1 \\ -1 & 2 \end{bmatrix}$

$A \cdot A^{-1} = \begin{bmatrix} 11 & -1 \\ -1 & 5 \end{bmatrix}$

$(A \cdot A^{-1})^{-1} = \begin{bmatrix} 11 & -1 \\ -1 & 5 \end{bmatrix} = A \cdot A^{-1}$

1
2
5
5
2

3.

$$A^2 = \begin{bmatrix} 8 & 4 & 1 \\ -2 & 3 & 5 \\ 11 & 17 & 19 \end{bmatrix}$$

$$3A = \begin{bmatrix} 9 & 3 & 0 \\ -3 & 3 & 3 \\ 6 & 9 & 12 \end{bmatrix}$$

$$2I = \begin{bmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{bmatrix}$$

$$A^2 - 3A + 2I = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 2 \\ 5 & 8 & 9 \end{bmatrix}$$

2

1

5 5

1

1

V

$$1. \left(x^2 - \frac{1}{x}\right)^5 = \sum_{r=0}^5 \binom{5}{r} (x^2)^{5-r} \left(\frac{1}{x}\right)^r$$

$$= \binom{5}{0} (x^2)^5 \left(\frac{1}{x}\right)^0 + \binom{5}{1} (x^2)^4 \left(\frac{1}{x}\right)^1 + \binom{5}{2} (x^2)^3 \left(\frac{1}{x}\right)^2$$

$$+ \binom{5}{3} (x^2)^2 \left(\frac{1}{x}\right)^3 + \binom{5}{4} (x^2)^1 \left(\frac{1}{x}\right)^4 + \binom{5}{5} (x^2)^0 \left(\frac{1}{x}\right)^5$$

$$= x^{10} - 5x^8 \cdot \frac{1}{x} + 10x^6 \cdot \frac{1}{x^2} - 10x^4 \cdot \frac{1}{x^3}$$

$$+ 5x^2 \cdot \frac{1}{x^4} - \frac{1}{x^5}$$

$$= x^{10} - 5x^7 + 10x^4 - 10x + \frac{5}{x^2} - \frac{1}{x^5}$$

2

2

5 5

1

2

$$n C_2 = 210$$

$$\frac{n(n-1)}{1 \cdot 2} = 210$$

$$n^2 - n - 420 > 0$$

$$(n-21)(n+20) = 0$$

$$\Rightarrow n = 21 \text{ or } n = -20$$

1

2

5 5

1

1

3.

$$\frac{\sin^2 \theta + (1 + \cos \theta)^2}{(1 + \cos \theta) \sin \theta}$$

1

$$\begin{aligned}
 &= \frac{\sin^2 \phi + 1 + 2 \cos \phi + \cos^2 \phi}{(1 + \cos \phi) \sin \phi} \\
 &= \frac{(\sin^2 \phi + \cos^2 \phi) + 1 + 2 \cos \phi}{(1 + \cos \phi) \sin \phi} \\
 &= \frac{2(1 + \cos \phi)}{(1 + \cos \phi) \sin \phi} \\
 &= \frac{2}{\sin \phi} = \underline{\underline{2 \csc \phi}}
 \end{aligned}$$

VI 1. r th term is the middle term

$$(r+1)^{\text{th}} \text{ term} = \binom{12-r}{r} (2a)^{12-r} \left(\frac{-b}{3}\right)^r$$

$$7^{\text{th}} \text{ term} = \binom{12}{6} (2a)^6 \left(\frac{b}{3}\right)^6$$

2.

$$\tan A = -\frac{8}{15}$$

$$\sin A = -\frac{8}{17}$$

$$\csc A = -\frac{17}{8}$$

$$\cos A = \frac{15}{17}$$

$$\sec A = \frac{17}{15}$$

3.

$$\text{L.H.S} = \frac{1 - \frac{1}{\sqrt{3}}}{1 + \frac{1}{\sqrt{3}}}$$

$$= \frac{\sqrt{3}-1}{\sqrt{3}+1}$$

$$= \frac{(\sqrt{3}-1)^2}{3-1}$$

$$= 2 - \sqrt{3}$$

vii

1.

$$\tan(A+B) = \tan \frac{\pi}{4} = 1$$

$$\frac{\tan A + \tan B}{1 - \tan A \tan B} = 1$$

$$\tan A + \tan B = 1 - \tan A \tan B$$

$$\tan A \tan B + \tan A + \tan B = 1$$

$$1 + \tan A \tan B + \tan A + \tan B = 2$$

$$(1 + \tan A)(1 + \tan B) = 2$$

55

2.

$$\tan^2 \frac{A}{2} = \frac{1 - \cos A}{1 + \cos A}$$

$$\tan^2 22\frac{1}{2}^\circ = \frac{1 - \cos 45^\circ}{1 + \cos 45^\circ}$$

$$= \frac{1 - \frac{1}{\sqrt{2}}}{1 + \frac{1}{\sqrt{2}}} = \frac{\sqrt{2} - 1}{\sqrt{2} + 1}$$

$$= \frac{(\sqrt{2} - 1)^2}{2 - 1}$$

$$= (\sqrt{2} - 1)$$

$$\tan 22\frac{1}{2}^\circ = \sqrt{2} - 1$$

55

3.

$$\tan\left(\frac{A-B}{2}\right) = \frac{a-b}{a+b} \cdot \cot \frac{C}{2}$$

$$\frac{a-b}{a+b} = \frac{2R \sin A - 2R \sin B}{2R \sin A + 2R \sin B}$$

$$= \frac{\sin A - \sin B}{\sin A + \sin B}$$

$$= \frac{2 \cos\left(\frac{A+B}{2}\right) \cdot \sin\left(\frac{A-B}{2}\right)}{2 \sin\left(\frac{A+B}{2}\right) \cdot \cos\left(\frac{A-B}{2}\right)}$$

$$= \frac{\cos\left(\frac{A-B}{2}\right)}{\sin\left(\frac{A+B}{2}\right)}$$

$$= \cot\left(\frac{A+B}{2}\right) \cdot \tan\left(\frac{A-B}{2}\right)$$

$$\tan\left(\frac{A-B}{2}\right) = \left(\frac{a-b}{a+b}\right) \cdot \tan\left(\frac{A+B}{2}\right)$$

$$= \left(\frac{a-b}{a+b}\right) \cdot \cot \frac{C}{2}$$

VIII

1.

$$\cos A = \frac{-4}{5}$$

$$\sin A = \frac{-3}{5}$$

$$\cos B = \frac{-12}{13}$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B = \frac{36}{65}$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B = \frac{63}{65}$$

2.

$$\cos 20^\circ \cdot \cos 40^\circ \cdot \cos 80^\circ = \frac{1}{2} (2 \cos 40^\circ \cdot \cos 20^\circ) \cos 80^\circ$$

$$= \frac{1}{2} (\cos 60^\circ + \cos 20^\circ) \cos 80^\circ$$

$$= \frac{1}{4} (\cos 80^\circ + \frac{1}{2} \cos 80^\circ \cos 20^\circ)$$

$$= \frac{1}{4} \cos 80^\circ + \frac{1}{8} (2 \cos 80^\circ \cos 20^\circ)$$

$$= \frac{1}{4} \cos 80^\circ + \frac{1}{4} (\cos 100^\circ - \cos 60^\circ)$$

$$= \frac{1}{4} \cos 80^\circ - \frac{1}{4} \cos 80^\circ + \frac{1}{8} = \frac{1}{8}$$

3.

$$\text{L.H.S} = ab^2 \cos A + ac^2 \cos A + bc^2 \cos B + ba^2 \cos B + ca^2 \cos C + cb^2 \cos C$$

$$= ab(b \cos A + a \cos B) + ac(c \cos A + a \cos C)$$

$$+ bc(c \cos B + b \cos C)$$

$$= abc + abc + abc = \underline{\underline{3abc}}$$

IX

1.

$$A = \cos^{-1} \left(\frac{b^2 + c^2 - a^2}{2bc} \right) = \cos^{-1} (0.8286) = 34^\circ 03'$$

$$B = \cos^{-1} \left(\frac{a^2 + c^2 - b^2}{2ac} \right) = \cos^{-1} (0.7143) = 44^\circ 25'$$

$$C = 180 - (A+B) = 101^\circ 32'$$

2.

$$m = \tan \theta = \tan 135^\circ = -1$$

$$(x_1, y_1) = (3, -4)$$

Equation is $y - y_1 = m(x - x_1)$

$$y - (-4) = -1(x - 3)$$

$$y + 4 = -x + 3$$

$$\underline{x + y + 1 = 0}$$

1		
1	5	
1		5
1		

3.

Point of Intersection $(-1, 0)$

Any line parallel to $x + y + 6 = 0$ is

$$x + y + k = 0$$

if passes through $(-1, 0)$

$$-1 + 0 + k = 0$$

$$k = -1$$

\therefore The equation is $\underline{x + y + 1 = 0}$

2		
1		5
1	5	5
1		

X 1.

$$\tan\left(\frac{A-B}{2}\right) = \frac{a-b}{a+b} \cot \frac{C}{2}$$

$$A - B = 38^\circ 13'$$

$$A + B = 110^\circ$$

$$A = 74^\circ 08'$$

$$B = 35^\circ 52'$$

$$\frac{a}{\sin A} = \frac{c}{\sin C}$$

$$c = \underline{84.99 \text{ cm}}$$

2		
1		5
1	5	5
1		

2.

$$2x - 3y + 5 = 0 \rightarrow ax + by + c = 0$$

$$\text{slope} = \frac{-a}{b} = \frac{-2}{-3} = \frac{2}{3}$$

$$x\text{-intercept} = -c/a = -5/2$$

$$y\text{-intercept} = -c/b = -5/-3 = 5/3$$

1		
2		
1	5	5
1		

3.

Any line \perp to $3x - 2y - 13 = 0$

is $2x + 3y + k = 0$

This line passes through $(0, 0)$

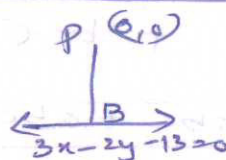
$$\therefore 2x + 3y + k = 0$$

$$\therefore k = 0$$

Point of Intersection of

$$3x - 2y - 13 = 0 \text{ and } 2x + 3y = 0$$

$$\text{is } (3, -2)$$



1		
1		
3	5	5