

SCORING INDICATORS

COURSE NAME : MATHEMATICS II

COURSE CODE : REV (21) - 2002

QID : 2106220099(A)

Qn. No.	Scoring Indicators	Split Score	Sub Total	Total Score
	PART A			9
I.1	$\sec^2 \theta - \tan^2 \theta = 1$		1	
I.2	$A+B = \begin{bmatrix} 1 & -2 \\ -1 & 2 \end{bmatrix}$		1	
I.3	$\hat{i} + 2\hat{j} + 4\hat{k}$ or $-\hat{i} - 2\hat{j} - 4\hat{k}$		1	
I.4	$\sqrt{2^2 + (-1)^2 + 2^2} = 3$		1	
I.5	$-\cos x + C$		1	
I.6	$\frac{x^3}{3} + 3x + C$		1	
I.7	$\left[\frac{3x^2}{2}\right]_0^1 = 3/2$		1	
I.8	Order = 2, degree = 1		1	
I.9	$dy = x^2 dx$, $y = \frac{x^3}{3} + C$		1	
	PART B			24
II.1	$x^2 - 36 = 0$, $x^2 = 36$, $x = \pm 6$	1+1+1	3	
II.2	$A^T = \begin{bmatrix} 3 & 0 \\ 1 & 1 \\ -1 & 2 \end{bmatrix}$ $AA^T = \begin{bmatrix} 3 \times 3 + 1 \times 1 + -1 \times -1 & 3 \times 0 + 1 \times 1 + -1 \times 2 \\ 0 \times 3 + 1 \times 1 + 2 \times -1 & 0 \times 0 + 1 \times 1 + 2 \times 2 \end{bmatrix} = \begin{bmatrix} 11 & -1 \\ -1 & 5 \end{bmatrix}$	1 1+1	3	
II.3	$\text{adj } A = \begin{bmatrix} 2 & -3 \\ 1 & 3 \end{bmatrix}$, $ A = 9$, $A^{-1} = \frac{\begin{bmatrix} 2 & -3 \\ 1 & 3 \end{bmatrix}}{9}$	1+1+1	3	
II.4	$\vec{a} \times \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 2 & -1 \\ 6 & -3 & 2 \end{vmatrix} = \hat{i}(4-3) - \hat{j}(4+6) + \hat{k}(-6-12) = \hat{i} - 10\hat{j} - 18\hat{k}$	1+1 1	3	
II.5	Displacement $\vec{AB} = \hat{i} + \hat{j} + 3\hat{k}$ Work done = $\vec{F} \cdot \vec{AB} = (\hat{i} + 2\hat{j} + \hat{k}) \cdot (\hat{i} + \hat{j} + 3\hat{k}) = 6 \text{ units}$	1 1 1	3	
II.6	$\vec{OP} = \hat{i} + 2\hat{j} + 3\hat{k}$, $\vec{OQ} = 3\hat{i} + 5\hat{j} + 6\hat{k}$ $\vec{PQ} = \vec{OQ} - \vec{OP} = 2\hat{i} + 3\hat{j} + 3\hat{k}$ $ \vec{PQ} = \sqrt{2^2 + 3^2 + 3^2} = \sqrt{22}$	1 1 1	3	
II.7	$\int \cos^2 x dx = \int \frac{1 + \cos 2x}{2} dx$ $= \frac{1}{2} \left[\int 1 dx + \int \cos 2x dx \right]$ $= \frac{1}{2} \left(x + \frac{\sin 2x}{2} \right) + C$	1 1 1	3	

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II.8	$\int x \sin x \, dx = x \int \sin x \, dx - \int \left[\frac{d}{dx}(x) \cdot \sin x \, dx \right] dx$ $= x(-\cos x) - \int 1(-\cos x) \, dx$ $= -x \cos x + \sin x + C$	1 1 1	3	
II.9	$\int_0^1 \frac{1}{1+x^2} \, dx = [\tan^{-1}x]_0^1$ $= \tan^{-1}(1) - \tan^{-1}(0)$ $= \pi/4 - 0 = \pi/4 \text{ (or } 45^\circ)$	1 1 1	3	
II.10	$\frac{dy}{dx} = e^{3x} \cdot e^y$ $e^{-y} dy = e^{3x} dx$ Integrating $-e^{-y} = \frac{e^{3x}}{3} + C$	1 1 1	3	
	PART C			42
III.1	$\Delta = \begin{vmatrix} 1 & 2 & -1 \\ 3 & 1 & 1 \\ 1 & -1 & 2 \end{vmatrix} = -3, \quad \Delta_1 = \begin{vmatrix} -3 & 2 & -1 \\ 4 & 1 & 1 \\ 6 & -1 & 2 \end{vmatrix} = -3$ $\Delta_2 = \begin{vmatrix} 1 & -3 & -1 \\ 3 & 4 & 1 \\ 1 & 6 & 2 \end{vmatrix} = 3, \quad \Delta_3 = \begin{vmatrix} 1 & 2 & -3 \\ 3 & 1 & 4 \\ 1 & -1 & 6 \end{vmatrix} = -6$ $x = \frac{\Delta_1}{\Delta} = 1, \quad y = \frac{\Delta_2}{\Delta} = -1, \quad z = \frac{\Delta_3}{\Delta} = 2$	1+1 1+1 1+1+1	7	
III.2	a) Equating corresponding elements, $a=2,$ $a+b=3, \therefore b=1$ $2a-c=7, \quad c=-3$ b) $A^T = \begin{bmatrix} 1 & 2 \\ -1 & -3 \end{bmatrix}$ $A+A^T = \begin{bmatrix} 1 & -1 \\ 2 & -3 \end{bmatrix} + \begin{bmatrix} 1 & 2 \\ -1 & -3 \end{bmatrix} = \begin{bmatrix} 2 & 1 \\ 1 & -6 \end{bmatrix}$	$\left. \begin{matrix} 1 \\ 1 \\ 1 \\ 2 \end{matrix} \right\} 4$ $\left. \begin{matrix} 1 \\ 1+1 \end{matrix} \right\} 3$	7	
III.3	a) $\vec{a} \cdot \vec{b} = 2 \times -2 + 1 \times 2 + 1 \times -3$ $= -4 + 2 - 3 = -5$ b) $\vec{BA} = \vec{r} = \hat{i} + \hat{j} + 4\hat{k}$ $\vec{BA} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 1 & 4 \\ 4 & 0 & -3 \end{vmatrix} = \hat{i}(-3-0) - \hat{j}(-3-16) + \hat{k}(0-4)$ $= -3\hat{i} + 19\hat{j} - 4\hat{k}$ moment = $ \vec{BA} \times \vec{F} = \sqrt{(-3)^2 + 19^2 + (-4)^2} = \sqrt{386} \text{ units}$	$\left. \begin{matrix} 1 \\ 1 \end{matrix} \right\} 2$ $\left. \begin{matrix} 1 \\ 1+1 \\ 1 \end{matrix} \right\} 5$	7	

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III.4	a) $\vec{a} + \vec{b} = 3\hat{i} - 2\hat{j} + \hat{k}$ $\vec{a} + \vec{b} = \sqrt{3^2 + (-2)^2 + 1^2} = \sqrt{14}$ unit vector = $\frac{\vec{a} + \vec{b}}{ \vec{a} + \vec{b} }$ $= \frac{3\hat{i} - 2\hat{j} + \hat{k}}{\sqrt{14}}$ b) $\vec{a} + \vec{b} = 3\hat{i}$ $\vec{a} - \vec{b} = -\hat{i} + 2\hat{j} + 2\hat{k}$ $(\vec{a} + \vec{b}) \cdot (\vec{a} - \vec{b}) = -3$	$\left. \begin{array}{c} 1 \\ 1 \\ 1 \\ 1 \end{array} \right\} 4$	7	
III.5	a) since, given vectors are $\perp$, their dot product = 0 ie, $8 + p + 2 = 0$ $\therefore p = -10$ b) $\vec{a} \times \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -1 & 2 \\ -1 & 1 & -1 \end{vmatrix}$ $= -\hat{i} - \hat{j}$ $\vec{a} \times \vec{b} = \sqrt{2}$ unit vector = $\frac{\vec{a} \times \vec{b}}{ \vec{a} \times \vec{b} } = \frac{-\hat{i} - \hat{j}}{\sqrt{2}}$	$\left. \begin{array}{c} 1 \\ 1 \\ 1 \end{array} \right\} 3$ $\left. \begin{array}{c} 1 \\ 1 \\ 1 \\ 1 \end{array} \right\} 4$	7	
III.6	a) $2\vec{a} = 2\hat{i} + 2\hat{j} + 2\hat{k}$ $3\vec{b} = 6\hat{i} - 3\hat{j} - 3\hat{k}$ $2\vec{a} \cdot 3\vec{b} = 12 - 6 - 6 = 0$ b) $\vec{AB} \times \vec{BC} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 3 \\ -3 & -2 & 1 \end{vmatrix} = \hat{i}(2+6) - \hat{j}(1+9) + \hat{k}(-2+6)$ $= 8\hat{i} - 10\hat{j} + 4\hat{k}$ $\vec{AB} \times \vec{BC} = \sqrt{180}$ Area = $\frac{1}{2} \vec{AB} \times \vec{BC} = \frac{1}{2} \sqrt{180}$ sq. units.	$\left. \begin{array}{c} 1 \\ 1 \\ 1 \end{array} \right\} 3$ $\left. \begin{array}{c} 1 \\ 1 \\ 1 \\ 1 \end{array} \right\} 4$	7	
III.7	a) put $u = x + \cos x$ $du = (1 - \sin x) dx$ $\int \frac{1 - \sin x}{x + \cos x} dx = \int \frac{du}{u}$ $= \log u + C = \log(x + \cos x) + C$ b) $\int_0^{\pi/2} \sin 2x dx = \left(-\frac{\cos 2x}{2} \right)_0^{\pi/2}$ $= -\frac{\cos \pi}{2} + \frac{\cos 0}{2} = -\frac{-1}{2} + \frac{1}{2}$ $= 1$	$\left. \begin{array}{c} 1 \\ 1 \\ 1 \\ 1 \end{array} \right\} 4$ $\left. \begin{array}{c} 1 \\ 1 \\ 1 \end{array} \right\} 3$	7	

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III.8	a) $\int x^2 \log x \, dx = \int \log x \cdot x^2 \, dx$ $= \log x \cdot \int x^2 \, dx - \int \frac{1}{x} \cdot \frac{x^3}{3} \, dx$ $= \frac{x^3 \log x}{3} - \frac{x^3}{9} + c$ b) $\int \sec x \, dx = \int \frac{\sec x (\sec x + \tan x)}{(\sec x + \tan x)} \, dx$ Put $u = \sec x + \tan x$ $du = \sec x (\sec x + \tan x) \, dx$ $\therefore \int \sec x \, dx = \int \frac{du}{u} = \log u + c = \log (\sec x + \tan x) + c$	1 1 1 } 3 1 1 1 } 4	7	
III.9	a) $\int \frac{3 \cos x + 4}{\sin^2 x} \, dx = \int \left(\frac{3 \cos x}{\sin^2 x} + \frac{4}{\sin^2 x} \right) \, dx$ $= 3 \int \left(\frac{1}{\sin x} \cdot \frac{\cos x}{\sin x} \right) \, dx + 4 \int \frac{1}{\sin^2 x} \, dx$ $= 3 \int \operatorname{cosec} x \cot x \, dx + 4 \int \operatorname{cosec}^2 x \, dx$ $= -3 \operatorname{cosec} x - 4 \cot x + c$ b) $\int_0^{\pi/2} \sin x \, dx = (-\cos x)_0^{\pi/2}$ $= -\cos(\pi/2) - (-\cos 0)$ $= -0 + 1 = 1$	1 1 1 } 4 1 1 1 } 3	7	
III.10	a) put $u = \sin x$ $du = \cos x \, dx$ $\int \sin^3 x \cos x \, dx = \int u^3 \, du$ $= \frac{u^4}{4} + c = \frac{\sin^4 x}{4} + c$ b) $\int_1^2 \log x \, dx = (x \log x - x)_1^2$ $= (2 \log 2 - 2) - (1 \log 1 - 1)$ $= 2 \log 2 - 1$	1 1 1 } 4 1 1 1 } 3	7	

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II.11	Intersecting points of parabola and x-axis is given by $y=0$ i.e. $x^2 - x - 2 = 0$ $x = -1, 2$ $\therefore \text{Area} = \int_{-1}^2 (x^2 - x - 2) dx = 0$ $= \left(\frac{x^3}{3} - \frac{x^2}{2} - 2x \right)_{-1}^2$ $= \left(\frac{8}{3} - \frac{4}{2} - 4 \right) - \left(-\frac{1}{3} - \frac{1}{2} + 2 \right)$ $= -9/6.$ Area = $9/2$ sq. units.	1 1 1 1 1 1	7	
III.12	Equation is of the form $\frac{dy}{dx} + Py = Q$ $P = \tan x$ I.F. = $e^{\int P dx}$ $= e^{\int \tan x dx}$ $= e^{\log(\sec x)} = \sec x.$ Multiply by I.F., the equation becomes $\frac{d(y \sec x)}{dx} = \cos^2 x \sec x dx = \cos x.$ Integrating both sides w.r.to x, $y \sec x = \int \cos x dx$ $y \sec x = \sin x + C$	1 1 1 1 1 1	7	