

**DIPLOMA EXAMINATION IN ENGINEERING/TECHNOLOGY/
MANAGEMENT/COMMERCIAL PRACTICE, NOVEMBER – 2024**

DISCRETE MATHEMATICS

[Maximum Marks: 75]

[Time: 3 Hours]

PART-A

I. Answer ‘all’ the following questions in one word or one sentence. Each question carries ‘one’ mark.

(9 x 1 = 9 Marks)

		Module Outcome	Cognitive level
1.	If A has n elements then number of subsets of A =.....	M1.01	R
2.	If p is a proposition $\neg(\neg p) = \dots\dots\dots$	M1.03	U
3.	$nP_n = \dots\dots\dots$	M2.02	U
4.	If $ A = m$ and $ B = n$ then $n(A \times B) = \dots\dots\dots$	M2.02	R
5.	If $f: A \rightarrow B$ is a function from A to B then A is called.....	M2.03	R
6.	A vertex which is not adjacent to every other vertex is called.....	M3.02	R
7.	A graph with p vertices and q edges is called.....	M3.02	R
8.	Every cyclic group is.....	M4.01	R
9.	Every subgroup of a cyclic group is.....	M4.01	R

PART-B

II. Answer any ‘eight’ questions from the following. Each question carries ‘three’ marks.

(8 x 3 = 24 Marks)

		Module Outcome	Cognitive level
1.	Find $A \cup B$ and $A \cap B$ if $A = \{2, 4, 7, 8\}$ and $B = \{4, 5, 6, 7\}$.	M1.01	U
2.	Determine the truth value of conjunction table.	M1.03	U
3.	Write all subsets $A = \{1, 2, 3\}$.	M1.01	U
4.	Find the number of permutations of the letters of the word INDEPENDENCE.	M2.02	U
5.	Let $f: \mathbb{R} \rightarrow \mathbb{R}$ where $f(x) = 3x + 7$ for all $x \in \mathbb{R}$. Prove that f is one-one.	M2.03	U
6.	How many edges are there in a graph with 10 vertices each of degree 6?	M3.02	A
7.	Define trees and spanning trees.	M3.03	R
8.	Define pre-order traversal.	M3.03	U
9.	Define (i) semigroup (ii) monoid	M4.01	U
10.	Let $A = \{a, b\}$. Draw the Hasse diagram of $(\mathcal{P}(A), \subseteq)$ and check whether it is a lattice.	M4.02	U

PART-C

Answer 'all' questions from the following. Each question carries 'seven' marks.

(6 x 7 = 42 Marks)

		Module Outcome	Cognitive level
III.	Draw appropriate Venn diagram for each of the following. (i) $(A \cup B)^c$ (ii) $A^c \cap B^c$ OR	M1.01	A
IV.	If A and B are two sets such that $A \cup B$ has 50 elements. A has 28 elements and B has 32 elements. How many elements does $A \cup B$ have?	M1.01	A
V.	Construct truth table for the compound statement $\neg (p \vee q) \rightarrow \neg p$. OR	M1.03	U
VI.	Use truth table $\neg (p \rightarrow q) \rightarrow \neg q$ is a logical implication.	M1.03	U
VII.	Let * be a binary operation on the set N of natural numbers defined by the rule $a*b = ab/4$ for all $a, b \in N$. Is * a) Commutative b) Associative. OR	M1.02	U
VIII.	Show that the function $f:N \rightarrow N$ given by $f(x)=2x$, is one -one and onto.	M2.03	U
IX.	An undirected graph has an even number of vertices of odd degree. OR	M3.02	U
X.	Show that the size of every graph of order n is atmost $n(n-1)/2$?	M3.02	U
XI.	Prove that every connected graph G has a spanning tree? OR	M3.03	U
XII.	Prove that the sum of degree of all vertices in G equal to twice the number of edges.	M3.02	U
XIII.	Show that $A = \{1, -1, i, -i\}$ is a group under multiplication. OR	M4.01	U
XIV.	Show that the set of integers under addition is a group.	M4.01	U
