

**DIPLOMA EXAMINATION IN ENGINEERING/TECHNOLOGY/
MANAGEMENT/COMMERCIAL PRACTICE, NOVEMBER – 2024**

MATHEMATICS - I

[Maximum Marks: 75]

[Time: 3 Hours]

PART-A

I. Answer *all* the following questions in one word or one sentence. Each question carries 'one' mark.

(9 x 1 = 9 Marks)

		Module Outcome	Cognitive level
1.	Find the conjugate of the complex number $1-i$	M1.01	U
2.	Find the slope of the straight line $3x - 2y + 1 = 0$	M1.02	U
3.	Evaluate $\sin 90^\circ \times \cos 0^\circ$	M2.01	U
4.	Find the value of $\sin 135^\circ$	M2.02	R
5.	Write the expression for $\sin 2A$ in terms of $\tan A$	M2.03	R
6.	Find $\lim_{\theta \rightarrow 0} \cos \theta$	M3.01	U
7.	Find $\frac{dy}{dx}$ if $y=e^x - \log x$	M3.03	U
8.	Find $\frac{dy}{dx}$ if $x^2+y=1$	M4.02	A
9.	Find the second derivative of $\log x$	M4.03	A

PART-B

II. Answer any *eight* questions from the following. Each question carries 'three' marks.

(8 x 3 = 24 Marks)

		Module Outcome	Cognitive level
1.	Multiply $(3 + i)$ with its conjugate.	M1.01	R
2.	Find the equation of the line with x intercept 3 and passing through the point $(-2, 3)$	M1.02	U
3.	If $\sec \theta = 2$ then find $\tan \theta$ and $\cot \theta$	M2.02	R
4.	If $\tan A = 2$ and $\tan B = 1$ then find $\tan(A+B)$ and $\tan(A - B)$	M2.03	U
5.	Prove that $(\cos A + \sin A)^2 = 1 + \sin 2A$	M2.03	U
6.	Show that $\lim_{\theta \rightarrow 0} \frac{\tan \theta}{\theta} = 1$	M3.02	U
7.	Find the derivative of $x \sin^{-1} x$.	M3.04	A
8.	If $x = 2t^3, y = 4t^2$ then find $\frac{dy}{dx}$.	M4.02	U
9.	Find $\frac{dy}{dx}$ if $x^3 + y^3 = 3x$	M4.02	U
10.	If $y = \sin x + \cos x$ then show that $\frac{d^2y}{dx^2} + y = 0$	M4.03	A

PART-C

Answer all questions from the following. Each question carries 'seven' marks

(6 x 7 = 42 Marks)

		Module Outcome	Cognitive Level
III.	i) Multiply the complex numbers $3 + 2i$ with itself. (4 marks)	M1.01	R
	ii) Find the modulus and amplitude of the complex number $3-4i$ (3 marks)	M1.01	R
OR			
IV.	i) Find the equation to the line parallel to $3x - y + 5 = 0$ and passing through $(3, -2)$ (4 marks)	M1.04	U
	ii) Find the point of intersection of the lines $x + y = 4$ and $x - y = 7$ (3 marks)	M1.03	U
V.	i) Evaluate $(1 + 2i)(2 - i) + (1 - 3i)(2 + i) - (5 - 2i)$. OR	M1.01	R
VI.	i) Find the angle between $x - y + 1 = 0$ and $\sqrt{3}x + y + \sqrt{2} = 0$. (4 marks)	M1.03	R
	ii) A straight line is inclined 45° with X-axis and passes through $(3, -4)$. Find the equation. (3 marks)	M1.02	R
VII.	i) If $\cos\theta = -\frac{4}{5}$, θ lies in the second quadrant then find all other trigonometric functions.	M2.02	U
	ii) Prove that $\frac{1+\cos 2A}{\sin 2A} = \cot A$ (5+2 marks)	M2.03	U
OR			
VIII.	Prove that i) $\sin(A + B) - \sin(A - B) = 2 \cos A \sin B$	M2.03	R
	ii) $\frac{\sin 3x}{\sin x} - \frac{\cos 3x}{\cos x} = 2$ (3 + 4 marks)	M2.03	R
IX.	Find i) $\lim_{x \rightarrow 0} \frac{\sin 2x}{\sin 4x}$	M3.02	U
	ii) $\lim_{x \rightarrow 3} \frac{x^3 - 27}{x^2 - 9}$ (3+4 marks)	M3.02	U
OR			
X.	i) Find the derivative of $\tan x$ using quotient rule. (5 marks)	M3.04	A
	ii) Find the derivative of $x^3 - 3\sqrt{x} + 5$ (2 marks)	M3.03	A

XI.	Find i) $\lim_{x \rightarrow 2} \frac{x^2 - 5x + 6}{x^2 + x - 6}$	(4 marks)	M3.02	U
	ii) $\lim_{x \rightarrow 0} \frac{\sin 3x}{x} \cos x$	(3 marks)	M3.02	U
OR				
XII.	Find the derivative of the following functions			
	i) $\frac{x+1}{x-1}$	(4 marks)	M3.04	U
	ii) $x \operatorname{cosec} x$	(3 marks)	M3.04	U
XIII.	Find the derivative of			
	i) $e^{2x} \sin 2x$	(4 marks)	M4.01	A
	ii) $\frac{\sin(\log x)}{x}$	(3 marks)	M4.01	A
OR				
XIV	Find $\frac{dy}{dx}$ if i) $x^2 + xy + y^2 = 0$	(4 marks)	M4.02	U
	ii) $x = t - \sin t, y = 1 - \cos t$	(3 marks)	M4.02	U
