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Scoring Indicators

COURSE NAME:HYDRAULICS

COURSE CODE :4011

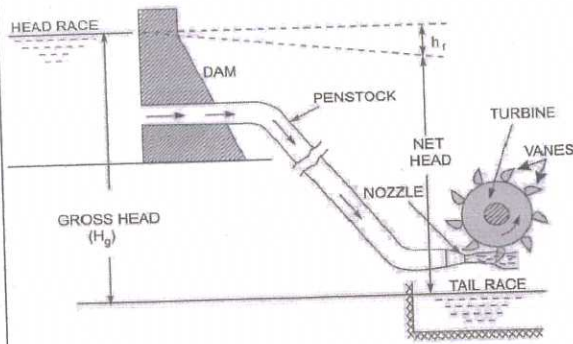
QID :1

Q No	Scoring Indicators	Split score	Sub Total	Total score
	<b>PART A</b>			<b>10</b>
I.1	<b>Surface Tension:</b> Surface tension is defined as the tensile force acting on the surface of a liquid in contact with the gas or on the surface between two immiscible liquids such that the contact surface behaves like a membrane under tension  <b>Capillarity:</b> Define the phenomenon of rise or fall of any liquid surface in a small tube relative to the adjacent general level of liquid when the tube is held vertically in the liquid		2	
I.2.	<b>Vena Contracta :</b> This term refers to a point within a fluid stream where the velocity of the fluid is at its maximum and the cross-sectional area is at its minimum		2	
I.3	a) Orifice: An orifice is a small, typically circular opening or hole in a surface, barrier, or device that allows fluids (liquids or gases) to pass through. Orifices are commonly used in engineering and fluid dynamics to control the flow of fluids or to measure the rate of flow b) Notch: A notch, refers to a specially shaped or configured opening or groove, often provided on the side of a container or channel, to allow the controlled discharge of fluid.	1  1	2	
I.4	The total energy line (TEL) is a graphical or mathematical representation used to represent the total energy of a fluid at various points along a flow path within a system. It shows the different forms of energy that a fluid possesses in a pipeline or open channel.  Total Energy (TE) = Kinetic Energy (KE) + Potential Energy (PE) + Pressure Energy (PE)	2	2	
I.5	The hydraulic mean depth is defined as the ratio of the cross-sectional area of flow (A) to the wetted perimeter (P). Mathematically, it is expressed as:  Hydraulic Mean Depth (HMD) = $A / P$  Where: • A - the cross-sectional area of the flow (the area of the water surface).	2	2	

	<ul style="list-style-type: none"> <li>• P - the wetted perimeter, which is the length of the channel bottom and sides that is in contact with the flowing liquid.</li> </ul>			
<b>PART B</b>				30
II.1	<p>Atmospheric Pressure:</p> <ul style="list-style-type: none"> <li>• Atmospheric pressure, also known as barometric pressure, is the pressure exerted by the Earth's atmosphere on any given point on the Earth's surface. It is the force per unit area exerted by the weight of the air above a particular location</li> </ul> <p>Gauge Pressure:</p> <ul style="list-style-type: none"> <li>• Gauge pressure is the pressure measured relative to atmospheric pressure. It represents the pressure difference between the measured pressure and atmospheric pressure. Gauge pressure can be positive or negative, depending on whether the measured pressure is greater than or less than atmospheric pressure.</li> </ul> <p>Absolute Pressure:</p> <ul style="list-style-type: none"> <li>• Absolute pressure is the pressure measured relative to a perfect vacuum (zero pressure). It includes the pressure of the fluid or gas itself and any additional pressure from the atmosphere. To calculate absolute pressure from gauge pressure, you add atmospheric pressure to the gauge pressure.</li> </ul>	2	2	6
II.2.	<p>Vacuum pressure, <math>p_{\text{vacuum}} = 650 \text{ mm of Hg}</math>  Atm pressure, <math>p_{\text{atm}} = 1.01325 \text{ bar}</math>  <math>1 \text{ mm of Hg} = 133.416 \text{ N/m}^2</math> and  <math>1 \text{ bar} = 10^5 \text{ N/m}^2</math>  Hence, <math>1 \text{ mm of Hg} = 133.416 \times 10^{-5} \text{ bar}</math></p> <p>The vacuum pressure in bar as <math>p_{\text{vacuum}} = 650 \times 133.416 \times 10^{-5} \text{ bar}</math>  <math>= .8672 \text{ bars}</math></p> <p>Using the relation, absolute pressure, <math>p_{\text{abs}} = p_{\text{atm}} - p_{\text{vacuum}}</math></p> $= 1.01325 - 0.8672$ $= 0.14605 \text{ bar}$	2	2	2

II.3.	<p>Orifice is a small opening of any cross-section (such as circular, triangular, rectangular etc.) on the side or at the bottom of a tank, through which a fluid is flowing. A mouthpiece is a short length of a pipe which is two to three times its diameter in length, fitted in a tank or vessel containing the fluid. Orifices as well as mouthpieces are used for measuring the rate of flow of fluid.</p> <p style="text-align: center;"><b>CLASSIFICATIONS OF ORIFICES</b></p> <p>The orifices are classified on the basis of their size, shape, nature of discharge and shape of the upstream edge. The following are the important classifications :</p> <ol style="list-style-type: none"> <li>1. The orifices are classified as <b>small orifice</b> or <b>large orifice</b> depending upon the size of orifice and head of liquid from the centre of the orifice. If the head of liquid from the centre of orifice is more than five times the depth of orifice, the orifice is called small orifice. And if the head of liquids is less than five times the depth of orifice, it is known as large orifice.</li> <li>2. The orifices are classified as (i) Circular orifice, (ii) Triangular orifice, (iii) Rectangular orifice and (iv) Square orifice depending upon their cross-sectional areas.</li> <li>3. The orifices are classified as (i) Sharp-edged orifice and (ii) Bell-mouthed orifice depending upon the shape of upstream edge of the orifices.</li> <li>4. The orifices are classified as (i) Free discharging orifices and (ii) Drowned or sub-merged orifices depending upon the nature of discharge.</li> </ol> <p>The sub-merged orifices are further classified as (a) Fully sub-merged orifices and (b) Partially sub-merged orifices.</p>	2	4	6
II.4	<p>► <b>7.4 HYDRAULIC CO-EFFICIENTS</b></p> <p>The hydraulic co-efficients are</p> <ol style="list-style-type: none"> <li>1. Co-efficient of velocity, <math>C_v</math></li> <li>2. Co-efficient of contraction, <math>C_c</math></li> <li>3. Co-efficient of discharge, <math>C_d</math></li> </ol> <p><b>Coefficient of velocity</b> is the ratio of actual velocity of the jet at vena contractor to the theoretical velocity of jet. It is usually denoted by <math>C_v</math></p> $C_v = \frac{v}{\sqrt{2gH}}$ <p><b>Coefficient of contraction:</b> it is the ratio of area of jet at win a contractor to the area of the orifice especially denoted using <math>C_c</math></p> $C_c = \frac{a_c}{a}$ <p><b>Coefficient of discharge</b> is the ratio of actual discharge from an orifice to the theoretical discharge from the orifice</p> $C_d = \frac{Q}{Q_{th}}$ $C_d = \frac{Q}{Q_{th}} = \frac{\text{Actual velocity} \times \text{Actual area}}{\text{Theoretical velocity} \times \text{Theoretical area}}$ $= \frac{\text{Actual velocity}}{\text{Theoretical velocity}} \times \frac{\text{Actual area}}{\text{Theoretical area}}$ $C_d = C_v \times C_c$	3 x 2 marks each	6	

II. 5



Layout of a hydroelectric power plant.

A hydroelectric power plant converts the energy of flowing water into electricity. The layout of a typical hydroelectric power plant consists of several key components and structures.

- Dam:
- Reservoir:
- Intake Structure:
- Penstock:
- Turbines:

3

3

II.6

The expression for discharge over a rectangular notch or weir is the same.

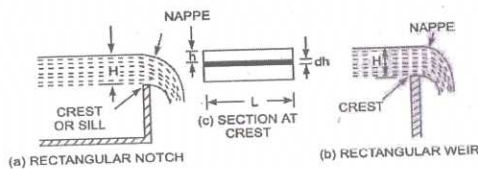


Fig. 8.1 Rectangular notch and weir.

Consider a rectangular notch or weir provided in a channel carrying water as shown in Fig. 8.1.

- Let  $H$  = Head of water over the crest
- $L$  = Length of the notch or weir

For finding the discharge of water flowing over the weir or notch, consider an elementary horizontal strip of water of thickness  $dh$  and length  $L$  at a depth  $h$  from the free surface of water as shown in Fig. 8.1(c).

The area of strip =  $L \times dh$   
and theoretical velocity of water flowing through strip =  $\sqrt{2gh}$

The discharge  $dQ$ , through strip is  
 $dQ = C_d \times \text{Area of strip} \times \text{Theoretical velocity}$  ... (i)  
 $= C_d \times L \times dh \times \sqrt{2gh}$

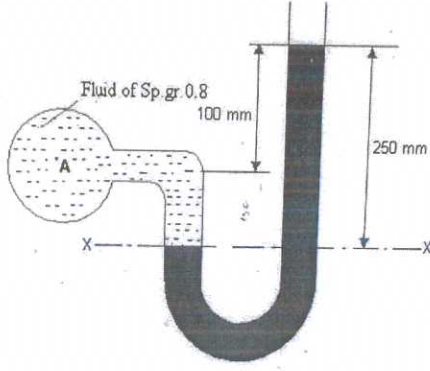
where  $C_d$  = Co-efficient of discharge.

The total discharge,  $Q$ , for the whole notch or weir is determined by integrating equation (i) between the limits 0 and  $H$ .

$$\begin{aligned} \therefore Q &= \int_0^H C_d \cdot L \cdot \sqrt{2gh} \cdot dh = C_d \times L \times \sqrt{2g} \int_0^H h^{1/2} dh \\ &= C_d \times L \times \sqrt{2g} \left[ \frac{h^{1/2+1}}{1/2+1} \right]_0^H = C_d \times L \times \sqrt{2g} \left[ \frac{h^{3/2}}{3/2} \right]_0^H \\ &= \frac{2}{3} C_d \times L \times \sqrt{2g} [H]^{3/2} \end{aligned} \quad \dots(8.1)$$

6



<p>III.b</p>	<p>Specific gravity of fluid in the pipe, <math>S_1 = 0.8</math></p> <p><math>\therefore</math> Density of the fluid, <math>\rho_1 = S_1 \times 1000 = 0.8 \times 1000 = 800 \text{ kg/m}^3</math></p> <p>Specific gravity of mercury, <math>S_2 = 13.6</math> (Assumed data)</p> <p><math>\therefore</math> Density of mercury, <math>\rho_2 = S_2 \times 1000 = 13.6 \times 1000 = 13600 \text{ kg/m}^3</math></p> <p>Height of mercury level in the right limb above XX or</p> <p>Difference of mercury level, <math>h_2 = 250 \text{ mm} = 0.25 \text{ m}</math></p> <p>Height of liquid in the left limb from X-X, <math>= 250 - 100 = 150 \text{ mm} = 0.15 \text{ m}</math></p>  <p style="text-align: center;"><b>I</b></p> <p>Let <math>p</math> be the intensity pressure of fluid flowing in pipe</p> <p>Equating the pressure at the left and right limb above the datum X-X, we get</p> $p + \rho_1 g h_1 = \rho_2 g h_2$ <p>Substituting the values in the above equation</p> $p + 800 \times 9.81 \times 0.15 = 13600 \times 9.81 \times 0.25$ $p + 1177.2 = 33354$ $p = 33354 - 1177.2 = 32176.8 \text{ N/m}^2 = 32.176 \text{ kN/m}^2$	<p>3</p> <p>1</p> <p>2</p> <p>3</p>	<p>9</p>	<p>9</p>
<p>IV. a.</p>	<p>1. Steady and Unsteady Flow:</p> <ul style="list-style-type: none"> <li>- Steady Flow: In a steady flow, the velocity and other flow characteristics at any given point in the fluid do not change with time.</li> <li>- Unsteady Flow: In unsteady flow, the fluid properties at a particular point change over time..</li> </ul> <p>2. Uniform and Non-Uniform Flow:</p> <ul style="list-style-type: none"> <li>- Uniform Flow: Uniform flow occurs when the fluid properties (e.g., velocity and pressure) are the same at all points within a particular cross-section of the flow. In other words, the flow does not vary along the direction of flow.</li> </ul>	<p>( 2 each x 3 = 6)</p>	<p>6</p>	<p>6</p>



VI.a

### EXPERIMENTAL DETERMINATION OF HYDRAULIC CO-EFFICIENTS

**Determination of Co-efficient of Discharge ( $C_d$ ).** The water is allowed to flow through an orifice fitted to a tank under a constant head,  $H$  as shown in Fig. . The water is collected in a measuring tank for a known time,  $t$ . The height of water in the measuring tank is noted down. Then actual discharge through orifice,

$$Q = \frac{\text{Area of measuring tank} \times \text{Height of water in measuring tank}}{\text{Time } (t)}$$

and theoretical discharge = area of orifice  $\times \sqrt{2gH}$

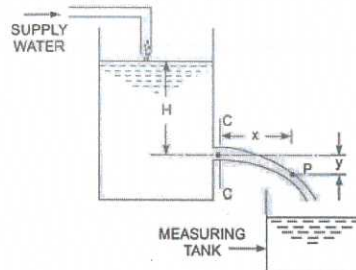


Fig. Value of  $C_d$ .

$$C_d = \frac{Q}{a \times \sqrt{2gH}}$$

**Determination of Co-efficient of Velocity ( $C_v$ ).** Let C-C represents the vena-contracta of a jet of water coming out from an orifice under constant head  $H$  as shown in Fig. . Consider a liquid particle which is at vena-contracta at any time and takes the position at P along the jet in time 't'.

Let  $x$  = horizontal distance travelled by the particle in time 't'

$y$  = vertical distance between P and C-C

$V$  = actual velocity of jet at vena-contracta.

Then horizontal distance,  $x = V \times t$  ... (i)

and vertical distance,  $y = \frac{1}{2} g t^2$  ... (ii)

From equation (i),  $t = \frac{x}{V}$

Substituting this value of 't' in (ii), we get

$$y = \frac{1}{2} g \times \frac{x^2}{V^2}$$

$$V^2 = \frac{g x^2}{2y}$$

$$\therefore V = \sqrt{\frac{g x^2}{2y}}$$

But theoretical velocity,

$$V_{th} = \sqrt{2gH}$$

$$\therefore \text{Co-efficient of velocity, } C_v = \frac{V}{V_{th}} = \frac{\sqrt{\frac{g x^2}{2y}}}{\sqrt{2gH}} = \sqrt{\frac{x^2}{4yH}}$$

$$= \frac{x}{\sqrt{4yH}}$$

**Determination of Co-efficient of Contraction ( $C_c$ ).** The co-efficient of contraction is determined from the equation (7.4) as

$$C_d = C_v \times C_c$$

$$\therefore C_c = \frac{C_d}{C_v}$$

7

2

3

2

VI.b	<b>Impulse turbine</b>	<b>Reaction Turbine</b>	1 mark each	8	
	The entire available energy of the water is first converted into kinetic energy.	The available energy of the water is not converted from one form to another.			
	The water flows through the nozzles and impings on the buckets, which are fixed to the outer periphery of the wheel.	The water is guided by the glide blades to flow over the moving vane.			
	The water impings on the buckets with KE	The water glides over the moving vanes with PE.			
	The pressure of the flowing water remains unchanged and is equal to the atmospheric pressure.	The pressure of the flowing water is reduced after gliding over the vane.			
	It is not essential that the wheel should run full.	It is essential that the wheel should always run full and kept full of water.			
	It is possible to regulate the flow without loss.	It is not possible to regulate the flow without loss.			
	Impulse Turbine has more hydraulic efficiency.	Reaction Turbine has relatively less efficiency.			
	Impulse Turbine operates at high water heads.	Reaction turbine operates at low and medium heads.			
	Example of Impulse turbine is Pelton wheel.	Examples of Reaction Turbine are Francis turbine, Kaplan and Propeller Turbine, Deriaz Turbine, Tubuler Turbine, etc.			
VII. a	<p>A triangular notch is preferred to a rectangular notch due to the following advantages over a rectangular notch.</p> <ol style="list-style-type: none"> <li>1. In a right angled V- notch the expression for the computation of discharge is very simple to remember (i.e., <math>Q = 1.417 \dots</math>)</li> <li>2. For measuring more accurate results for low discharge, triangular notch is preferred than rectangular notch</li> <li>3. In case of triangular notch, only one reading i.e., head (<math>H</math>) is required to be taken for the computation of discharge.</li> <li>4. No need for ventilation of triangular notch.</li> <li>5. The same triangular notch can measure a wide range of flows accurately.</li> <li>6. The head over the crest of triangular notch is independent of wetted edge. In case of rectangular notch the width or length of notch crest is constant for all heads with which the results are effected.</li> </ol>		7	7	
VII. b	<p>Discharge over the notch, <math>Q = 233 \text{ litres/s} = 0.233 \text{ m}^3/\text{s}</math></p> <p>Head over the notch, <math>H = \frac{1}{3} L</math></p> <p>Coefficient of discharge, <math>C_d = 0.62</math>.</p> <p>Using the equation for discharge, i.e., <math>Q = \frac{2}{3} C_d \cdot L \cdot \sqrt{2g} \cdot H^{\frac{3}{2}}</math></p> <p>Substituting</p> $0.233 = \frac{2}{3} \times 0.62 \times L \times \sqrt{2 \times 9.81} \times \left(\frac{L}{3}\right)^{\frac{3}{2}} = 0.352 \times L^{\frac{5}{2}}$ <p>∴ Length of the notch, <math>L = \left(\frac{0.233}{0.352}\right)^{\frac{2}{5}} = 0.85 \text{ m}</math></p>		1 1 1 2 2 1	8	



<b>LOSS OF ENERGY (OR HEAD) DUE TO FRICTION</b>				
<p>(a) Darcy-Weisbach Formula. The loss of head (or energy) in pipes due to friction is calculated from Darcy-Weisbach equation which has been derived and is given by</p> $h_f = \frac{4 \cdot f \cdot L \cdot V^2}{d \times 2g}$				
IX b.	<p>Diameter of pipe, <math>d</math> = 200mm = 0.2m  Length of pipe, <math>l</math> = 600m  Loss of head, <math>h_f</math> = 30m  Pipe friction coefficient, <math>f</math> = 0.01</p> <p>Using the Darcys formula for considering all minor losses.</p> $h_f = \frac{0.5v^2}{2g} + \frac{4flv^2}{2gd} + \frac{v^2}{2g} = \frac{v^2}{2g} \left( 0.5 + \frac{4fl}{d} + 1 \right)$ $30 = \frac{v^2}{2 \times 9.81} \left( 0.5 + \frac{4 \times 0.01 \times 600}{0.2} + 1 \right)$ $30 = \frac{v^2}{2 \times 9.81} \times 121.5$ $\therefore v = \sqrt{\frac{30 \times 2 \times 9.81}{121.5}} = 2.2 \text{ m/s}$ <p>According to the continuity equation</p> <p>Discharge through the pipe, <math>Q = a \times v = \frac{\pi}{4} d^2 \times v = \frac{\pi}{4} \times (0.2)^2 \times 2.2 = 0.0691 \text{ m}^3/\text{s}</math>  = 69.1 litres/s <span style="float: right;">(Ans)</span></p>	2	8	
	$h_f = \frac{0.5v^2}{2g} + \frac{4flv^2}{2gd} + \frac{v^2}{2g} = \frac{v^2}{2g} \left( 0.5 + \frac{4fl}{d} + 1 \right)$ $30 = \frac{v^2}{2 \times 9.81} \left( 0.5 + \frac{4 \times 0.01 \times 600}{0.2} + 1 \right)$ $30 = \frac{v^2}{2 \times 9.81} \times 121.5$ $\therefore v = \sqrt{\frac{30 \times 2 \times 9.81}{121.5}} = 2.2 \text{ m/s}$	4		
	<p>Discharge through the pipe, <math>Q = a \times v = \frac{\pi}{4} d^2 \times v = \frac{\pi}{4} \times (0.2)^2 \times 2.2 = 0.0691 \text{ m}^3/\text{s}</math>  = 69.1 litres/s <span style="float: right;">(Ans)</span></p>	2		
X.a.	<p>Diameter of pipe, <math>d</math> = 250 mm = 0.25m  Length of pipe, <math>l</math> = 100m  Velocity of flow, <math>v</math> = 2.5 m/s  Coefficient of pipe friction, <math>f</math> = 0.005  Chezy's constant, <math>C</math> = 55</p> <p>Using Darcy's formula</p> <p>Head loss due to friction, <math>h_f = \frac{4flv^2}{2gd} = \frac{4 \times 0.005 \times 100 \times (2.5)^2}{2 \times 9.81 \times 0.25}</math>  = 2.548 m of water <span style="float: right;">(Ans)</span></p> <p>Hydraulic mean depth, <math>m = \frac{d}{4} = \frac{0.25}{4} = 0.0625 \text{ m}</math></p> <p>Loss of head per unit length, <math>i = \frac{h_f}{l} = \frac{h_f}{100}</math></p> <p>Using Chezy's formula for velocity of flow,</p> $v = C \sqrt{mi}$ <p>Substituting</p> $2.5 = 55 \times \sqrt{0.0625 \times \frac{h_f}{100}}$ $\therefore h_f = \left( \frac{2.5}{55} \right)^2 \times \frac{100}{0.0625} = 3.306 \text{ m of water} \quad (\text{Ans})$	2	7	
	<p>Head loss due to friction, <math>h_f = \frac{4flv^2}{2gd} = \frac{4 \times 0.005 \times 100 \times (2.5)^2}{2 \times 9.81 \times 0.25}</math>  = 2.548 m of water <span style="float: right;">(Ans)</span></p>	2		
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